Accurate Aggregation of Local Features by using K-sparse Autoencoder for 3D Model Retrieval

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Abstract

Aggregating a set of local features has been used widely to realize recognition or retrieval of multimedia data including 2D images and 3D models. A number of feature aggregation algorithms (e.g., Bag-of-Features [5], Locality-constrained Linear coding [26], or Fisher Vector coding [23]) have been proposed. They first learn a codebook, or a set of codewords, by clustering the local features and then encode these local features by using the learned codebook. Despite the great success of these feature aggregation algorithms, we argue that they are not necessarily optimal in terms of accuracy since their codebook learning and feature encoding are computed separately. In this paper, we propose two novel feature aggregation algorithms based on k-Sparse Autoencoder (kSA) [20] that realize more accurate local feature aggregation. Our proposed algorithms, called Database-adaptive kSA (DkSA) and Per-data-adaptive kSA (PkSA) aggregation, jointly optimize codebook learning and feature encoding. In addition, the kSA-based feature encoding enhances saliency of local features due to k-sparseness constraints and non-negativity constraints. Of the two proposed algorithms, the PkSA aggregation exploits reconstruction error of a local feature derived from the kSA for more accurate aggregated feature. Experimental evaluation using a shape-based 3D model retrieval scenario showed that the retrieval accuracy of our proposed algorithms are superior to the existing feature aggregation algorithms we have compared against.

Keywords

Feature aggregation, feature encoding, autoencoder, sparse coding, local feature, bag-of-features, content-based retrieval, 3D shape.

1. INTRODUCTION

Aggregation of local features is an important technological component for effective and efficient comparison among multimedia data objects, including 2D images, 3D models, etc. Recently, for the task of classification or retrieval of 2D images, “end-to-end” deep learning has achieved higher accuracy than the conventional approach which combines hand-crafted local features and their aggregation. On the other hand, recent studies (e.g., [10]) have shown that aggregating features derived from a deep neural network is also effective for 2D image retrieval. Also, for shape-based 3D model retrieval (3DMR) on which we focus in this paper, extracting local features from a 3D model and aggregating them per 3D model remains as one of the most promising approaches. We thus think that improving feature aggregation is still quite meaningful for progress of multimedia information retrieval.

Goal of local feature aggregation is to generate a feature vector that reflects, as well as possible, distribution of local features in their feature space. Feature aggregation generally consists of two steps, i.e., encoding and pooling. A set of codewords are chosen, typically, by clustering the set of local features. A local feature is encoded by using codewords around the feature and statistics associated with the codewords. Such statistics as density, mean, and/or variance, can be used for the encoding. For pooling, encoded local features are accumulated into a single feature per 3D model. For efficient inter-feature comparison, aggregated feature better be compact.

Many algorithms for feature aggregation have been proposed [12]. They can be roughly classified into two groups: sparse coding (SC)-based approach and higher-order statistics (HS)-based approach. The SC-based approach (e.g., [5][19][26]) sparsely encodes a local feature by using weighted linear sum of its neighboring codewords. Locality-constrained Linear (LL) coding [26] is one of the most representative SC-based methods. Bag-of-Features (BF) [5] is a special case of the SC-based approach in which a local feature is assigned to its nearest single codeword by vector quantization. On the other hand, the HS-based approach (e.g., [14][23][27]) tries to encode local features by using higher-order statistics around the codewords. Fisher Vector (FV) coding [23] employs mean and variance of local features around the codeword. Vector of Locally Aggregated Descriptor (VLAD) [14] approximates the FV by using only mean around the codeword.

These feature aggregation algorithms described above have been successfully utilized for recognition or retrieval of 2D images or 3D models. However, they are not necessarily optimal in terms of accuracy since the codebook learning and the feature encoding steps are processed separately. That is, as a pre-processing, a codebook (i.e., a set of codewords) is first learned by clustering the set of local features. Then, each local feature is encoded by using the learned codebook. This “greedy” framework is adopted by most of the feature aggregation algorithms including BF, LL1, FV, VLAD, and Triangular Encoding (TE) [4]. The greedy approach could reduce expressive power of the aggregated features.

1 Although joint optimization framework is proposed in [26], LL is typically used along with a codebook learned by k-means clustering in the literature.
In this paper, aiming for more accurate aggregation of local features, we propose a pair of novel SC-based feature aggregation algorithms. The algorithm is based on k-Sparse Autoencoder (kSA) proposed by Makhzani et al. [20]. A kSA-based feature aggregation can be more accurate than the existing ones for two reasons. Firstly, kSA can jointly optimize codebook learning and feature encoding as kSA is trained by alternating encoding of local features and updating of codewords (i.e., updating of connection weights of kSA neurons) so that reconstruction error of the local features is minimized. Similar joint optimization framework is employed by Sparse Autoencoder (SA) [21] and KSVD [2], which are popular sparse coding algorithms. Secondly, feature encoding by kSA could enhance saliency of local features since the kSA has two constraints considered to aid accurate feature encoding, that are, k-sparse-ness and non-negativity. K-sparse-ness constrains feature encoding to use a small number (k) of codewords correlated to the local feature. Non-negativity forces coefficients weighting the codewords to be non-negative. Several state-of-the-art SC-based algorithms, e.g., LL coding and Localized Soft-assignment (LS) coding [19], showed these constraints improve accuracy of encoded features.

Our two kSA-based feature aggregation algorithms are called Database-adaptive kSA (DkSA) aggregation and Per-data-adaptive kSA (PkSA) aggregation. DkSA (Figure 1b) is a straight-forward approach for feature aggregation using kSA. As a pre-processing (Figure 1a), kSA is trained by using numerous and diverse local features sampled from the database (hence database-adaptive). After training, each of a set local features extracted from a 3D model is encoded by using the database-adapted kSA. The set of encoded local features are accumulated into a single feature vector per 3D model by sum-pooling for efficient comparison. PkSA (Figure 1c), on the other hand, aims at generating aggregated features more expressive than DkSA by exploiting reconstruction error of local features derived from the kSA. kSA is first trained in the same manner as DkSA (Figure 1a). Then, the database-adapted kSA is additionally trained, or fine-tuned, by using a set of local features extracted from each 3D model (hence per-data-adaptive).

An aggregated feature for the 3D model is a set of displacements of parameters, or weights, caused by the fine-tuning. Table 1 compares characteristics of SC-based feature aggregation algorithms we will evaluate in the experimental section. The DkSA and the PkSA have potential to yield expressive aggregated features since both of them satisfy all the criteria essential for accurate feature aggregation, i.e., joint optimization of codebook and feature encoding, k-sparse constraint, and non-negative constraint. Exploiting reconstruction error of local features for PkSA is novel for the group of SC-based feature aggregation algorithms.

Experimental evaluation under a 3DMR scenario shows that the proposed kSA-based feature aggregation algorithms significantly outperform existing SC-based and HS-based counterparts.

Contributions of this paper can be summarized as follows.

- Proposition of two k-Sparse Autoencoder based feature aggregation algorithms, that are, DkSA and PkSA, for more accurate aggregation of local features.
- Quantitative evaluation of DkSA and PkSA using multiple local features and multiple benchmark datasets for 3DMR.

## 2. PROPOSED ALGORITHM

### 2.1 Database-adaptive kSA Aggregation

As with the previous feature aggregation methods, DkSA (Figure 1b) aggregation consists of two processing steps, that are, encoding and pooling of local features. At the encoding stage, a set of local features extracted from a 3D model is first normalized by using ZCA-whitening [3] so that local features have zero means and all the pair of dimensions are uncorrelated. Then, each whitened local feature is fed into the trained kSA to obtain unit activations in the hidden layer. Feature encoding is performed as \( h = \sigma(y) = \sigma(W_s x) \), where \( h \) is an encoded local feature (or unit activation in the hidden layer), \( x \) is a input (whitened) local feature, \( W_s \) is a weight matrix for encoder, and \( \sigma \) is a non-linear activation function. By using hidden layer with \( n \) units, \( d \)-dimensional local feature \( x \) is encoded into \( n \)-dimensional feature \( (n > d) \). Note that our kSA includes bias terms for both encoder and decoder, although the bias term is omitted from the equation for notation simplicity.

Activation function \( \sigma \) strongly influences saliency of encoded local features. Our activation function consists of Rectified Linear Units (ReLU) [16] and \( k \)-largest value selection. Specifically, \( y_i \), which is \( i \)-th element of \( y \), is first rectified by using ReLU, i.e., \( z_i = \max(0, y_i) \). ReLU ensures non-negativity of feature encoding. Then, \( k \) largest elements in \( \{z_i | i = 1, \ldots, n\} \) are kept while the rest is set to 0.

At the pooling stage, the set of encoded local features is aggregated into a single feature vector per 3D model by summing. Therefore, the number of dimensions for aggregated feature is also \( n \). Finally,
the aggregated feature vector is normalized by using power normalization followed by L2 normalization as with [23]. Cosine similarity is used to compare a pair of DkSA-aggregated features.

DkSA has two hyper-parameters that require manual tuning, i.e., the number of units in the hidden layer $n$ and the number of non-zero elements in the hidden layer $k$. In the experiments, $n$ is typically set to 8,000 and small $k$ (e.g., $k=3$) is used.

Training of the kSA is performed as follows. The kSA is trained by minimizing mean squared reconstruction error of local features. We use $T=250k$ local features randomly sampled from the database for training. We use Stochastic Gradient Descent (SGD) with mini-batch. Each mini-batch contains 200 local features randomly selected from the set of $T$ training local features. To adaptively assign a learning rate to each parameter (i.e., each connection weight between neurons), we use AdaGrad algorithm [6] with an initial learning rate $= 0.2$. Training is regularized with weight decay coefficient $\lambda = 10^{-4}$. The optimization is iterated for 50 epochs.

2.2 Per-data-adaptive kSA Aggregation

P\(k\)SA (Figure 1c) aims at generating more accurate aggregated features than D\(k\)SA by exploiting reconstruction error of local features. For pre-processing, kSA is trained in the same manner as DkSA except for the initial learning rate = 0.05 for AdaGrad. We use this initial learning rate since it yielded slightly higher retrieval accuracy in the preliminary experiments.

To aggregate a set of local features extracted from a 3D model $M$, the database-adapted kSA is additionally trained, or fine-tuned, by using the local features of the 3D model $M$. The kSA parameters $W_k$ for encoder and $W_d$ for decoder are fine-tuned to reconstruct the local features of the 3D model $M$. Then, we compute displacement, or differential, of parameters due to fine-tuning as $\Delta W = W_k^* - W_k$, where $W_k^*$ and $W_k$ indicate weight matrices of the decoder after and before fine-tuning, respectively. The displacement matrix $\Delta W$ is then vectorized to form a P\(k\)SA-aggregated feature for the 3D model $M$. The P\(k\)SA-aggregated feature vector has $D=n(n+1)/2$ dimensions where $n+1$ means that our kSA has bias terms. We can also use parameter displacement of the encoder, i.e., $\Delta W = W_d^* - W_d$ for aggregation. However, preliminary experiments showed that decoder displacement $\Delta W$ consistently outperformed encoder displacement $\Delta W$.

Note that fine-tuning for P\(k\)SA aggregation is performed per 3D model. That is, the database-adapted kSA is duplicated for each 3D model, and each duplicated kSA is fine-tuned by using the set of local features extracted from the 3D model. For fine-tuning, we employ Steepest Descent (SD) algorithm; all the local features of the 3D model are used to compute gradients of the parameters. We use SD instead of SGD (with mini-batch) so as to exclude randomness from the result of fine-tuning. We use AdaGrad with initial learning rate = 0.05 and fine-tuning is iterated for 50 epochs.

Since P\(k\)SA aggregation produces higher-dimensional aggregated feature vectors than DkSA aggregation, we perform dimension reduction of the P\(k\)SA-aggregated features for efficient inter-feature comparison. We use Sparse Random Projection (SRP) [1] algorithm to compress the P\(k\)SA-aggregated features down to 8,000 dimensions. Preliminary experiments showed that the SRP down to 8,000 dimensions did not degrade retrieval accuracy. Comparison among the dimension-reduced P\(k\)SA-aggregated feature vectors is done in a manner identical to that of DkSA; aggregated features are power-normalized and then L2-normalized for Cosine similarity.

P\(k\)SA has the same hyper-parameters as D\(k\)SA, i.e., the number of units in the hidden layer $n$ and the number of non-zero elements in the hidden layer $k$. In the experiments, $n$ is to 500 and $k$ is set to around 10, which is slightly larger than $k$ for DkSA.

3. EXPERIMENTS AND RESULTS

3.1 Experimental Setup

To validate efficacy of the proposed feature aggregation algorithms, we use four benchmark databases for 3DMR; the Princeton Shape Benchmark (PSB) [24], the Engineering Shape Benchmark (ESB) [13], the SHREC 2011 Non-Rigid watertight meshes dataset (SH11NR) [17], and the SHREC 2014 Large-scale Comprehensive 3D shape retrieval dataset (SH14LC) [18]. For all the benchmarks, one of 3D models in the database is used as a query and remaining 3D models are used as retrieval targets. We use Mean Average Precision (MAP) [%] as an index of retrieval accuracy. Since optimization of the proposed algorithms using SGD have randomness, all the experiments for DkSA and P\(k\)SA are performed three times and their average MAP are reported. Table 2 summarizes the number of non-zero units $k$ used for D\(k\)SA and P\(k\)SA aggregation. For another hyper-parameter, i.e., the number of hidden units, we use $n=8,000$ for D\(k\)SA and $n=500$ for P\(k\)SA unless otherwise stated.

| Table 2. Number of non-zero units $k$ used for experiments. |
| --- | --- | --- | --- | --- | --- |
| Feature Aggregation Algorithm | POD | LSF | SI | RoPS | DSIFT | MO1SIFT |
| DkSA | 5 | 5 | 5 | 5 | 5 | 5 |
| P\(k\)SA | 20 | 10 | 10 | 20 | 5 | 20 |

We compare the proposed feature aggregation algorithms against six existing feature aggregation algorithms, i.e., BF [5], LL [26], FV [23], VLAD (VL) [14], SV [27], and DM [9]. We also apply three sparse coding algorithms to local feature aggregation, i.e., Sparse Autoencoder (SA) [21], Triangular Encoding (TE) [4], and K-SVD [2]. For sparse coding-based aggregation methods including BF, LL, SA, TE, and K-SVD, we learn 8k codewords. On the other hand, for higher-order statistics-based methods including VL, FV, and SV, the number of codewords are determined so that dimensionality of aggregated feature vector becomes about 300k. For DM, we use 250k local features to generate a manifold graph for aggregation. All the aggregated feature vectors are power-normalized and are then L2-normalized. We use Cosine similarity for comparison among feature vectors.

We use six local features for 3DMR, i.e., Position and Orientation Distribution (POD) [9], Spin Image (SI) [15], Local Statistical Feature (LSF) [22], Rotational Projection Statistics (RoPS) [10], Dense SIFT (DSIFT) [7], and Multi-Orientation One SIFT (MO1SIFT) [8]. They are classified into two groups; local 3D geometric feature including POD, SI, LSF, RoPS, and local 2D visual feature including DSIFT and MO1SIFT. Each local feature extraction method has hyper-parameters, e.g., the number of local features per 3D model or the number of rendering views. In this paper, we follow the experimental settings by Furuya et al. [9].

3.2 Experimental Results

3.2.1 Comparison with Other Feature Aggregation Algorithms

Table 3 compares the proposed feature aggregation algorithms against the other feature aggregation algorithms for the PSB dataset. Part of the table is due to [9]. Table 3 shows our kSA-based feature aggregation algorithms outperform the existing SC-based methods, i.e., BF, SA, TE, K-SVD, and LL. We try to explain the results by using Table 1. TE has non-negativity but it lacks $k$-sparseness for feature encoding. K-SVD has $k$-sparseness (we used $k=5$ for the experiment) and it learns codebook and feature encoding jointly.
However, feature encoding by KSVD could produce negative coefficients. LL has both \(k\)-sparseness (we used \(k=15\)) and non-negativity. But feature encoding would be not optimal because it uses a codebook learned by \(k\)-means clustering. In comparison, the D\(k\)SA and P\(k\)SA satisfy both \(k\)-sparseness and non-negativity of feature encoding. Also, D\(k\)SA and P\(k\)SA jointly optimize codebook learning and feature encoding. P\(k\)SA outperforms D\(k\)SA for five out of six features in Table 3 as the former exploits reconstruction error of local features for aggregation.

Table 3 also shows D\(k\)SA and P\(k\)SA outperform the state-of-the-art HS-based aggregation methods for most cases. Joint optimization framework of the proposed algorithms would produce more accurate aggregated features than the “greedy” approach adopted by the HS-based methods in Table 3.

![Figure 2. Comparison of feature aggregation methods (PSB).](image)

<table>
<thead>
<tr>
<th>Algorithms</th>
<th>Pre-processing</th>
<th>Feature aggregation per 3D model</th>
</tr>
</thead>
<tbody>
<tr>
<td>BF</td>
<td>41.5</td>
<td>0.04</td>
</tr>
<tr>
<td>SV</td>
<td>342.6</td>
<td>0.08</td>
</tr>
<tr>
<td>D(k)SA</td>
<td>798.6</td>
<td>0.29</td>
</tr>
<tr>
<td>P(k)SA</td>
<td>226.9</td>
<td>0.75</td>
</tr>
</tbody>
</table>

Table 5 compares efficiency of feature aggregation algorithms. In the table, pre-processing for VL and SV mean learning a codebook with \(3k\) codewords. Meanwhile, pre-processing for D\(k\)SA and P\(k\)SA includes whitening of local features and training \(\text{ASA}\). Table 5 shows that D\(k\)SA and P\(k\)SA are accelerated by using a GPU. We use our own implementations based on the CUDA library for D\(k\)SA and P\(k\)SA.

In the experiments above, we used the only one benchmark database, i.e., the PSB. Table 4 shows generalization capability of the proposed algorithms for a variety of 3D model databases described in Section 3.1. We use POD local feature for the experiment. Table 4 shows the P\(k\)SA aggregation performs well, but not always the best, among the previous state-of-the-art feature aggregation algorithms.

3.2.2 Efficiency

We evaluate efficiency of the proposed \(\text{ASA}\)-based feature aggregation algorithms. We use a PC having two Intel Xeon E5-2650V2 CPUs, 256GB DRAM, and a GeForce GTX 980 GPU.

![Figure 2. Comparison of feature aggregation methods (PSB).](image)

In the experiments above, we used the only one benchmark database, i.e., the PSB. Table 4 shows generalization capability of the proposed algorithms for a variety of 3D model databases described in Section 3.1. We use POD local feature for the experiment. Table 4 shows the P\(k\)SA aggregation performs well, but not always the best, among the previous state-of-the-art feature aggregation algorithms.
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6. REFERENCES